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INTERMOLECULAR POTENTIALS OF **EDA COMPLEXES BY SEMI-EMPIRICAL** THEORY DISPERSION ENERGY TERMS IN THE PM3 METHOD

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Abstract; The recently developed PM3 parametrization scheme for MNDO**type calculations by Stewart is shown to glve ground state propertles (geometrles. energies oi formation) of the complexes rormed between TCNE and a varlety of aromatic donors In qualltatlve agreement wlth ab lnitlo and avallable experlmental results, provlded appropriate dlsperslon energy terms are Included. The method appears to yleld geometrles for EDA complexes** suitable for electronic structure calculations.

INTRODUCTION

Despite the development of ever-more faster computers and the advent of ready-to-use *ab initio* programs the calculation of molecular complexes even of moderate size will remain, for **years to come, a domain of empirical or semi-emplrlcal methods. These methods, as a consequence of suitable parametrlzatlon, are able to avold some of the pitfalls of the** *ab* **fnftfo me**thod, as there are the basis set superposition error,¹ the tendency to underestimate exchange repulsion caused by basis functions decaying too rapidly,² and the error due to neglect of cor**relation energy. Correlation energy, or rather the lack of It. is thought to be the reason that no stable complexes are calculated for the face-to-face interaction between two ethylene3 or benzene molecules4 at the single-determlnant Hartree-Fock level; even with the very flexible** 6-31G* basis no potential energy minimum develops between two approaching ethylenes.⁵ Elec**tron donor acceptor (EDA) complexes, e.g. between benzene and carbonyl cyanide, do not fare much better? calculated blndlng energies are much too small and distances too large, a consequence of inadequate representation of the intermolecular attraction.**

In Hartree-Fock theory to account for correlation energy ln the supermolecule approach of molecular complexes one can elther perform a conventlonal CI calculation or use a Moller-Plesset type perturbatlon approach7 both of which are rather time-consuming. There are other ways to improve on ab *initio*, viz. the use of emplrical energy terms to substitute or supple**ment the quantum-mechanical calculation .* In the Buckingham-Fowler model' the electrostatic** interaction between two molecules is calculated by using sets of distributed multipoles obtained **from** *eb fnftfo* **wave functions of the monomers. Morokuma from hls method of partionlng SCF Interaction energies¹⁰ has derived dispersion energy terms from second-order perturbation** theory¹¹ which are added onto a normal ab initio calculation of the supermolecule.¹² More in **line wlth this latter approach is the work by Hulszoon and Mulder'3. who fitted a long range**

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attractive r.exp (-6) term to ab initio calculated dispersion interaction coefficients. Their parameters which were corrected later¹⁴ have been used since in ab initio^t as well as in semiempirical calculations of intermolecular interactions¹⁵.

Much effort **has gone** into applying semi-empirical methods to the calculation of moleculsr complexes: CNDO/2¹⁶, CNDO/S¹⁷, PPP¹⁸, INDO¹⁹, as well as the more recent MNDO and AM1 models^{5,13} all have been used for this purpose. It is well known that of these methods CNDO and INDO cannot be employed to optimize supermoiecule structures because **of** their neglect of dlatomlc differential overlap. Thls **leads** to a loss of exchange repulsion and **as** a consequence calculated intermolecular distances are much too small. That MNDO and AM1 on the other hand are able to sufficiently reproduce repulsion between molecules or molecular fragments is due to their extensive parametrization, especially with **respect to** electrostatic repulsion. fntermolecular potentials have been calculated **by both** *8b fnftio* and MNDO. 8 Inclusion of dispersion via Muider's parameters ¹⁸ resulted in satisfactory potential energy curves for several EDA complexes; with AM1, the third-generation parametrization scheme,²³ on the other hand, no geometry optimization was possible.

MNDO today appears to be one of the most widely used semi-empirical methods²⁰. Recently Stewart has publlshed *an* improved parameter set **for** MNDO and AM1 called MNDO-PM321, which significantly reduces the error in calculated heats of formation. Since this method can be ex pected to find widespread acceptance we felt it appropriate to investigate the performance of MNDO-PM3 augmented with atomic **dispersion energy parameters.** The complexes we **have chosen** for this study, different aromatic systems and tetracyanoethylene (TCNE), **reflect our experimental approach** *to* EDA complex electronic structure: chiral derivatives **of** anthracene make the complexation with TCNE amenable to chiroptical techniques. By studying such complexes by UV and CD spectroscopy we hope to reveal more information about the interaction between the components.

METHOD

For the monomers either X-ray (TCNE) or MMP2-optimlzed structures (donor molecules) were used; these structures remained unchanged during optimization of the dlfferent complexes. For calculating the intermolecular potentials we employed PM3 as well as other methods $(MNDO^{22}$, AM1²³, both from QCPE²⁴ and ab *initio* as Gaussian 86²⁵). Atomic dispersion parameters were those published by Hobza and Zahradnik.²⁶ All conformations were strictly cofacial, i.e. the planes of the two n-components were always kept parallel. Energy calculations were performed with varylng distances between the molecular planes, until a minimum could be located. In addition, some **in-plane** motions were also considered.

RESULTS AND **bISCUSStON**

Because of its small size the benzene-TCNE complex lent itself not only to the different **semlempirical and standard** STO-3G calculations, but to split valence-orbital basis **Sets as Well** (STO-3-21G and STO-4-31G). These are the most advanced calculations reported so far for this complex. Watanabe²⁷ calculated this complex with the same basis, but the intermolecular

distance was not optimized, and the number of two-electron-lntegrals **wa6** considerably reduced.

There are two conformations with over-all C_{xy} -symmetry that are interconverted by a 30^o rotation of either component about the principal axis (1a, 1b). Energies and equilibrium distances obtained by the different methods are compared In Table 1. Blndlng energles range from 1.27 kcal/mol (MNDO) to 11.38 (STO-3G wlth dlsperslon energy added); only the *ab fnftlo* split-valence basis sets give energies that seem realistic even without added dispersion

VD signlrles added dlsperslon; bcalculated sum of SCF-energies of components (no Interaction), In kcal/mol for the semi-empirical. In a.u.'s for the *eb fnftfo* methods; tin kcal/mol; *in pm.

energy when compared with the experimental heat of formation which is 6.6 ± 0.3 kcal/mol in the gas phase or rather the binding energy which is $\emptyset.6$ kcal/mol less.²⁸.

In Fig. 1 the potential energy curves obtalned by the three *eb fnftfo* basls sets for the complex in are shown for comparison; also, the PM3 curve is included. Split-valence bases generally give SCF energles larger than $STO-3G₁$ ²⁹ because of the presumed tendency of these bases to overestimate charge effects (total charge on TCNE at 320 pm distance is .004. .018. and .016 8 for STO-3G. 4-316. and 3-21G. respectively). Obviously. electron density can transfer into the opposite fragment without experiencing sufficient repulsion, a consequence of both the greater range and flexiblllty of the split basis. Another indication of the somewhat unreallstlc charge distrlbutlon obtained wlth thls basis 1s the fact that the energy of the LUMO (which Is, of course, mostly TCNE-based) actually drops upon complexatlon; only in STO-3G and in PM3 the energy of thls MO rises. as one would expect.

_Fin. 1; SCF **energies of benzene-TCNE complex** $\frac{f(R)-f_1}{f(R)}$ as a function of intermolecular distance function, containing additional attractive and (1a) as a function of intermolecular distance for $\frac{f(R)}{R}$ ($\frac{f(R)-f_1}{R}$) and $\frac{f(R)-f_1}{R}$ ($\frac{f(R)-f_1}{R}$) an $21G$; $(+-+)$, STO-4-31G.

STO-3C. on the other hand, underestlmatee repulslon at these distances due to the rapld decay of the wave-function, 2.39 so the potential energy function turns out to be rather shallow. Compared to STO-3G PM3 is more repulsive except at very long distances; there **la a** croeslng of the two potential curves at 380 pm.

Calculated energy differences between la and lb are very small. as expected for what 1s essentially a 6-fold rotational barrier. All ab initio methods favor la slightly over 1b, while the opposite **1s** true for the semi-emplrlcal methods. AM1-calculated interaction energies are slgnlflcantly larger than **MNDO. a** direct \overline{R} 380 \overline{R} 480 consequence of parametrization. AM1 differs \overline{R} (pm) from MNDO only in the enlarged core repulsion repulsive Gaussian functions. This is supposed to make up for known weaknesses of MNDO,

e.g. failure to reproduce hydrogen bonds. In contrast, electronic energy calculations are identlcal. except, of course, for the parameters employed. Thls shows In our calculations: the dlfference In electronic energy between AM1 and MNDO stays almost constant over the whole intermolecular distance covered (800 to 260 pm); in contrast, the core-core repulsion calculated by AM1 drops rapidly compared to MNDO at distances below 35 β pm, leading to increased binding energies in this region. PM3 which also utilizes the expanded core repulsion function gi ves results identical with AM1 at the calculated equilibrium distance; at shorter distances, however, the AM1 energles rlse much slower than the one calculated by PM3. This Is of major consequence when we consider the addition of dispersion energy terms (see below).

To study the influence of configuration interaction we performed extensive AM1-CI calculations. Uslng a wlndow of 10 NO's (which **la** necessary to ensure the lncluslon of all relevant norbltals of the two components, vfz. 4 NO's for benzene. 2 MO's for **TCNE.)** and 1 600 up to quadruply excited conflguratlons. the stablllzatlon of la relative to Isolated benzene and TCNE amounts to only .24 kcal/mole. a result worse than without CI and undoubtedly due to an unbalanced description of electron correlation in the complex vs. the components. With a smaller number of excited configurations, no stabilization of the complex was obtained at all. This unsatisfactory performance of CI in calculations of this kind has been noted before¹⁵ and led to its substitution by dispersion energy terms in the first place.

The dispersion energy is obtained independent of the model used to calculate the electronic structure of the complex; it is a term that decreases monotonically with decreasing intermolecular separatlon. All energy mlnlma are therefore shifted towards smaller distance, the degree

dependlng only on the steepness of the potential energy function. The results are dlsplayed in Fig. 2; calculated values for the equilibrium geometries are given in Table 1. The small STO-3G basis set gives rather large interaction energies of more than 11 kcal/mol; also, the cal-

Fig. 2: Blndlng energy E of la as a function of intermolecular distance R. $('-')$, MNDO; $(+-+)$, PM3; $(x-x)$, AM1; $(o-o)$, STO-3G, all calculated with dispersion energy.

culated distance of 300 pm seems to be a rather small value. Due to the shallow potential energy curve calculated with AM1 no mlnlmum is obtained when dlspersion terms are added: the system collapses. MNDO gives a minimum, which is, however, rather flat (binding energy of about 3 kcal/mole at 380 pm). Between these two methods PM3 appears to present an acceptable compromise (7.1 kcal/mol at an equlllbrlum distance of 310 pm). Its energy curve running almost parallel to the STO-3G curve.

For the naphthalene-TCNE complex an X-ray crystal analysis has been performed: 31 one of

the conformations found is close to the Ideal geometry 2a, wlth an Intermolecular separatlon of 329 pm. The binding energy in the gas-phase has been determined $(7.1 \text{ kcal/mol}/^{27})$, somewhat larger than for the benzene complex. We have optimized the internuclear distance of the four structures 2a through 2d with STO-3G and PM3 lncludlng dlsperslon energy terms. In Tab. 2 blndlng energies and equlllbrlum distances are shown and, for a given intermolecular distance (320 pm) the different energy terms that make up the total energy. In this way a comparison of the methods applied is more meaningful.

Of the four conformations 2a is found to be the most stable by STO-3G and 2d by PM3; the difference in energy, however, between these and the least stable forms (2c and 2a) is very small, amounting to only 1.8 and \emptyset .6 kcal/mol, respectively. PM3 favors both C_{2v} over the C_5 geometries. Just the opposite of what STO-SC does. The term responslble for this 1s the dispersion energy, which 1s larger for **the more crowded geometrles.** Just llke the nuclear repulsion, which has a similar distance dependence. Subtracting this term from the binding energy gives the SCF energy, which, according to both methods, is more favorable for the less symmetric structures 2a and 2b.

*calculated at 320 pm distances between molecular planes; ba.u.'s for STO-3G, eV for PM3 (core repulslon); dat equlllbrlum distance (entry below, in pm).

The binding energy presents a delicate balance between (repulsive) nuclear and (attractive) electronic energy terms, of the two components compared with the complex. Conslderlng that the semi-empirical and the ab initio method yield absolute values for these terms differing even in magnitude, it is surprising how close the relative energies agree: the order of decreasing nuclear repulsion and electronic energy (2d, 2c, 2a, 2b) is ldentlcal according to both methods. Despite thls the two methods come to different results wlth respect to the SCF-energies because of the subtle differences Involved.

Nothlng is known concerning the binding energy or geometry of the anthracene-TCNE complex. By rotating and by moving the TCNE molecule over the plane of the aromatlc system

we found 3a the most stable conformation by STO-3G and 3b by PM3.

In Fig. 3 the potential energy curves for the naphthalene and the anthracene complexes with TCNE on the basis of STO-3G and PM3 are compared. The correspondence between thls semiemplrlcal and the *eb lnftfo* method Is agaln evldent: both favor the anthracene over the

naphthalene complex (and the latter over the benzene complex). and calculated STO-3G binding energies are always larger, by about the same factor. No high-quality ab *initio* calculations were possible for systems this size.

Fig. 3: Binding energy E of naphthalene-TCNE complex, $2a$ (-1) and anthracene-TCNE complex, 3a (---) vs. intermolecular distance R. Circles correspond to STO-3G, crosses to PM3 calculations, all including dispersion energy.

As a final test for the valldlty of the proposed method we have calculated the blndlng energies of TCNE with several methyl-substituted benzenes, for which energies of formation have been determined.²² Again only the intermolecular distances were varied, keeping the two molecules ln parallel planes. For each complex, two different geometries were calculated In which the TCNE molecule was rotated by 90°, except for 6 for which there were three starting geometries; only the most stable conformatlons are shown below.

Equlllbrlum distances and the energy terms making up the total blndlng energies are given In Table 3. All calculated distances lle between 310 and 330 pm. which seem to be reasonable values conslderlng the experimental geometry of the naphthalene-TCNE complex. Also, calculated blndlng energies represent experimental trends very well.

Introduction of methyl groups lowers the SCF energy of the benzene molecule substantially. Nevertheless, SCF binding energies for ldentlcal distances (not shown In the Table) rise In golng from 1 to 8. because the complexes get more crowded, and the increase In nuclear repulsion is not balanced by an equal increase in electronic energy. However, since the dispersion energy becomes more negatlve wlth the larger systems over-all blndlng energy Increases from 1 to 8. in general agreement with experiment.

The wrong order of stabilities is calculated for the two isomeric xylene-TCNE complexes.

According to our calculations the ortho-isomer 6 has an Intermolecular distance of 328 pm due to unfavorable interaction of the TCNE molecule with the two methyl groups (no geometry optimization was performed with respect to methyl torsion]. In the pars-isomer 5 the compo-

	1b	48	6а	6Ъ	7Ъ	8b
distance	310	310	310	320	330	330
SCF energy	200.130	191.650	183.180	183.383	172.396	166.191
SCF binding energy ^c	6.18	6.54	6.87	6.26	4.80	5.69
dispersion energy	-13.30	-14.72	-16.12	-14.66	-13.96	-15.43
binding energy	-7.12	-8.18	-9.25	-8.40	-9.10	-9.75
expt. energy. ^d	-6.0	-6.66	-7.42	-7.80	-9.09	-10.12

Tab. 3: Equilibrium distances² and energy terms³ of TCNE complexes

***in pm; bin kcal/mol; *SCF energy minus sum of SCF energies of components; arei.32.**

nents approach to within 31% pm which makes. of course, ior a **large gain in dispersion energy. Either moving the TCNE molecule in 6 away from the two methyl groups, or tilting its plane (motions not effective in lowering the energy of 6) should considerably stabilize this complex.** We **have applied only two criteria. binding energles and lntermoiecular dletances, to assess the validity of the method we propose. These criteria, as Judged from the sparse experimental data available, are met for the TCNE complexes. We have looked only superflclaliy at the electronic** structures of the complexes and found the data controversial. The PM3-calculated total **negative charge on the TCNE fragment at 320 pm distance from the aromate Increases from 302 to .0026 to .0038 e In going from benzene** (la) **to naphthalene** (2a) **to anthracene** (3a); **LUYO destablllzatlon for the complexes in the same order increases from .ll to .23 to .24 eV. Both these sequences indicate increasing interaction between the two components; however, HOMO energy shifts do not follow a clear pattern at all, possibly because other lower lying orbital8 are involved ln this stablllzatlon 6s well.**

We would like to make one final point regarding the distinction between a molecular complex **and a molecule proper. From the standpoint of SCF-theory. i.e. within the variational approach to molecular structure calculation. there Is no prlnclple difference between these two; most lmportant, the correlation energy is missing in both cases at the single determinant Hartree-Pock** level. For the calculation of molecular complexes this is known to present a serious flaw (vide supra); bonding may simply not occur. This deficiency does not show up with such consequence **in molecular structure calculations where bonding la provided per se and where "only* potential lunctlons may be changed somewhat.**

The question to what extent atomic dispersion terms might suffice to substitute for CI calculations, especially in large flexible molecules, has to our knowledge never systematicallY been pursued. We are presently engaged in addressing this problem.

CONCLUSION

There 1s an obvlous need for a fast and rellable method to calculate ground state geometrles of EDA complexes (or, for that matter, of any molecular complexes). EDA complexes have been postulated as precursors in cycloaddition reactions, like the Diels-Alder reaction, 33 or in certain elimination reactions.³⁴ To what extent the stereochemistry of such reactions is determined by the preference of the precursor complex for certain conformatlons may not be known until a complete conformational analysis, most probably on the basls of theoretical methods, has been performed.

Using a well established set of atomic dlsperslon energy parameters to supplement seml-empirical schemes we have looked closely at the three presently most popular methods, MNDO, AM1, and PM3. to see how they describe simple aromate-TCNE complexes and find the following: (1) MNDO underestlmates bondlng and glves complexes with Intermolecular distances too large.

As a consequence steric effects may be underrepresented.

(11) AM1 glves potential energy curves which are not repulsive enough to prevent collapse of the components once the dispersion terms are added.

(iii) PM3 results are evidently more realistic than the above giving reasonable intermolecular distances; experimental (gas-phase) binding energles are slightly over-estimated.

Whether these conclusions hold in general and for weakly bound molecular complexes as well will have to be seen; preliminary calculations³⁶ on the co-facial ethylene dimer and on the benzene-ethylene complex **using** PM3 and Hobza's parameters have yielded reasonable bindlng energies (1.13 and 3.0 kcal/mol) and equilibrium distances (310 and 290 pm, respectively).

Calculations were performed at the Hochschulrechenzentrum Duisburg.

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